

# Privacy-Enhancing Technologies

## Module 3: Database Anonymization

Thorsten Strufe

30.05.2022 – hybrid, KIT and TUD

*Disclaimer: This lecture was prepared in cooperation with*

*Patricia Arias-Cabarcos, Javier Parra-Arnau, and input from the people at the chair*



KASTEL Security Research Labs



# Statistical Disclosure Control

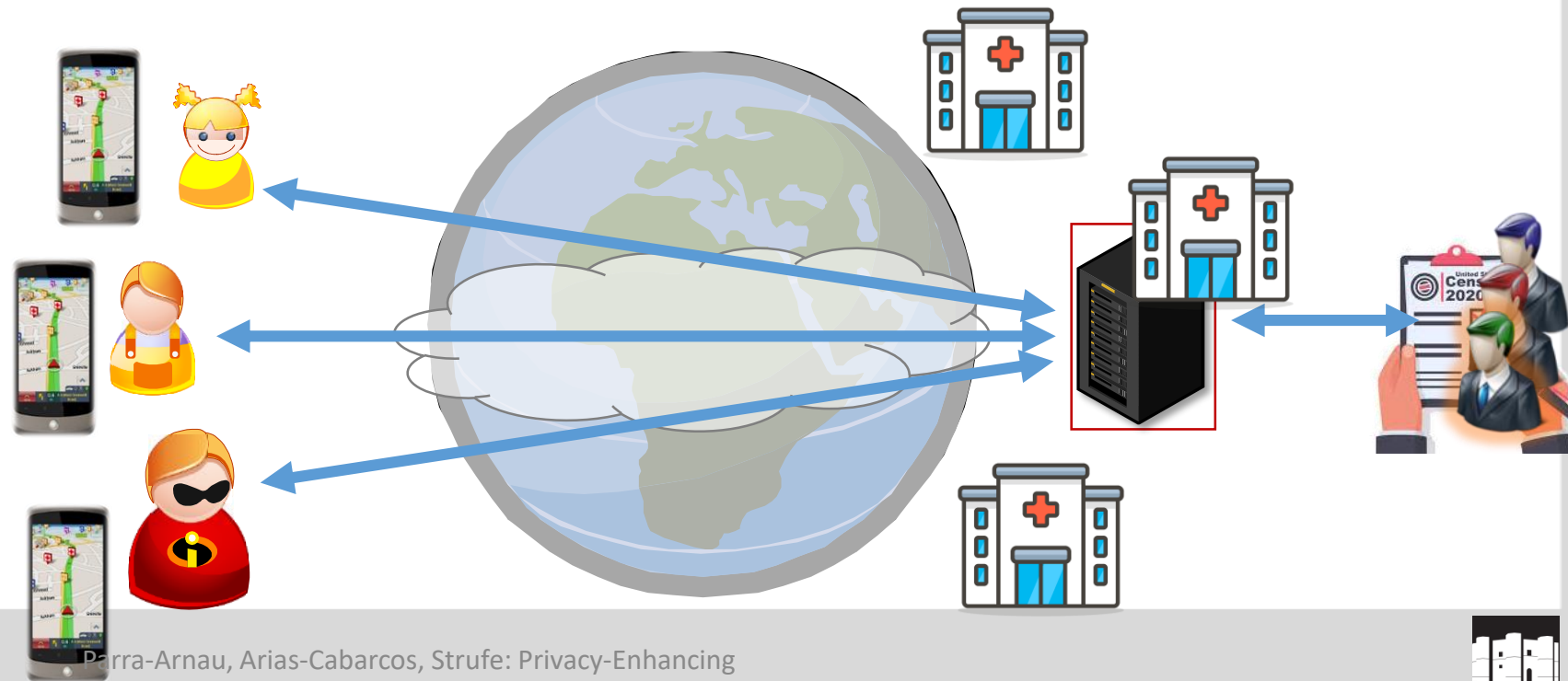
- Statistical disclosure control (SDC) is the **field** that protects statistical databases so that they can be released **without revealing confidential information** that can be linked to specific individuals among those to which the data correspond
- Seek to provide **useful statistical information** while guaranteeing respondent privacy is not compromised

- Three formats

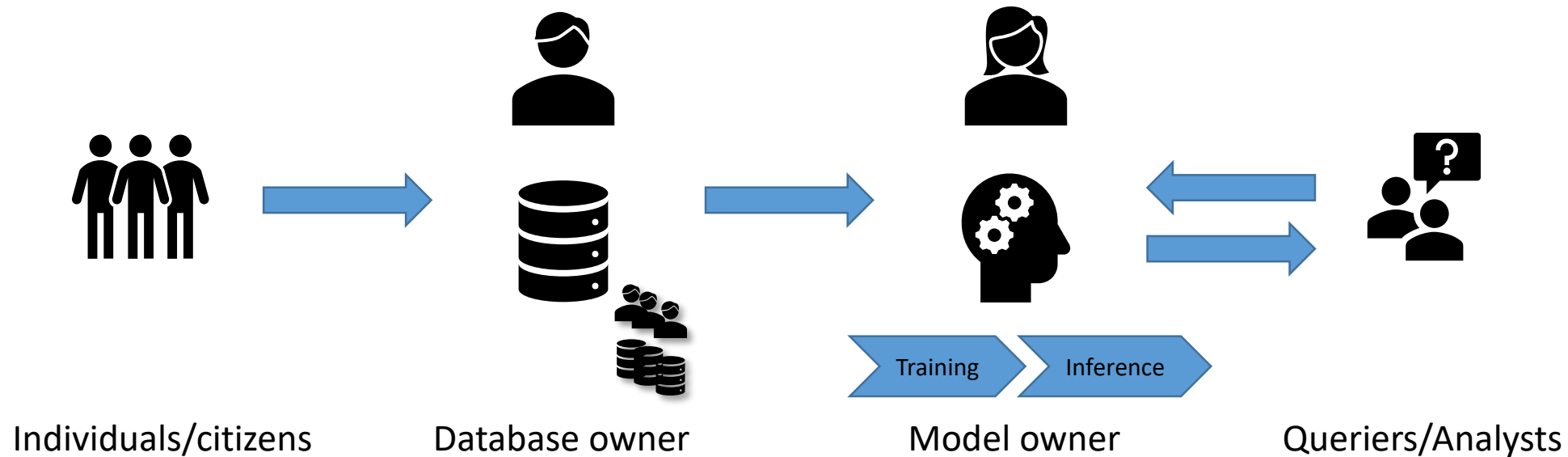
- Tabular
- Queryable
- Microdata

- Techniques

- Syntactic SDC
- Semantic SDC



# SDC vs PPDM vs PIR



- **SDC** aims to provide respondent privacy
- Privacy-preserving data mining (**PPDM**) seeks database owner privacy
- Private information retrieval (**PIR**) aims for user/analyst privacy

<sup>1</sup> A. Hundepool, J. Domingo-Ferrer, L. Franconi, S. Giessing, E. Schulte Nordholt, K. Spicer and P.-P. de Wolf (2012) Statistical Disclosure Control, Wiley.

# SDC applications

- Areas of application of SDC techniques include:
  - **Official statistics**
    - US Census Bureau
  - **Health information**
    - HIPAA in the U.S. and similar rules in other western countries
    - Increasing push towards medical data exchange (genomics, biosignals, ...)
  - **E-commerce**
    - Secondary purpose is restricted

# Database formats

- Tabular data
  - publish **static aggregate** information without disclosing confidential information on specific individuals
- Queryable databases
  - **Aggregate information** obtained by an analyst should not reveal information at the individual level
- Microdata
  - **Perturbed the original database** so as to keep the analytical usefulness of the data, while avoid respondent linkage

# Tabular data protection

- Tabular data

- **Magnitude table.** Sum of a particular response across a subset of respondents. E.g., turnover of all businesses of a particular industry within a region
- **Frequency table.** Number of respondents satisfying certain criteria. E.g., number of respondents in a city who suffer from a given condition

# Disclosure attacks on tabular data

- External attack

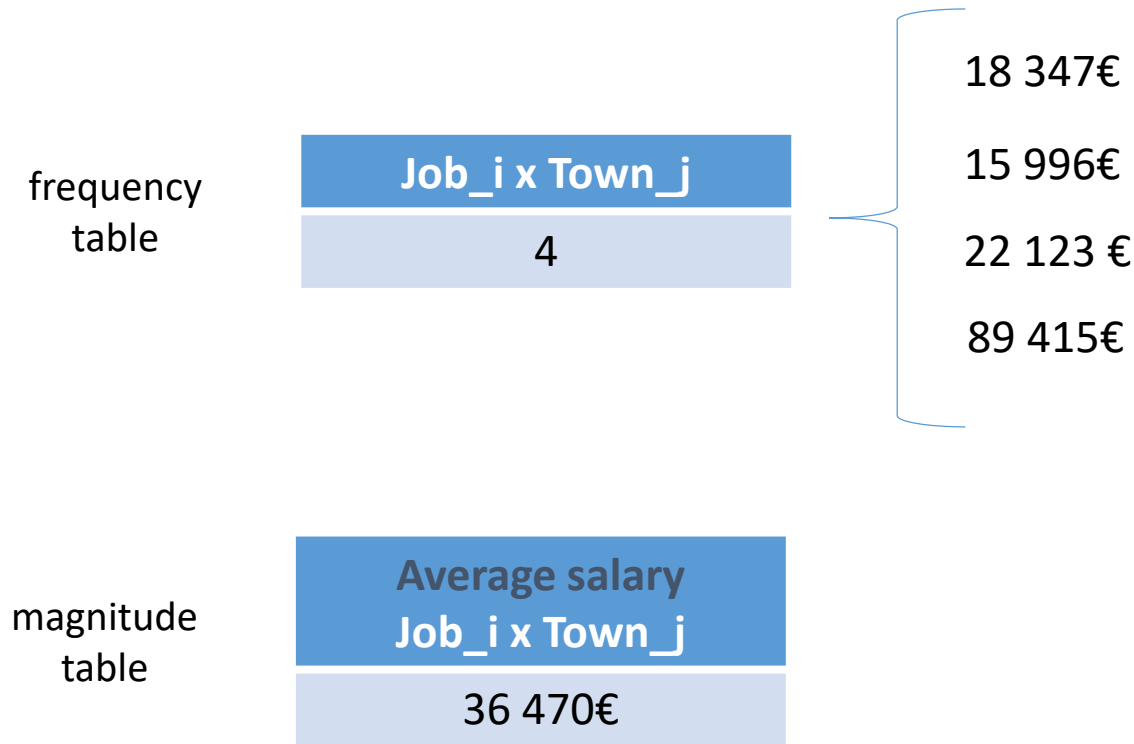
frequency table	<b>Job<sub>i</sub> x Town<sub>j</sub></b>	<b>Job<sub>j</sub> x Town<sub>j</sub></b>
	1	36
magnitude table	<b>Average salary Job<sub>i</sub> x Town<sub>j</sub></b>	<b>Average salary Job<sub>j</sub> x Town<sub>j</sub></b>
	18 347€	45 000€

- Internal attack

- Having two respondents is not enough

# Disclosure attacks on tabular data

- Dominance attack





# $k$ -Anonymity and Disclosure Attacks on Microdata

Identifying Attribute ← Quasi-identifier → Sensitive attribute

Name	DOB	Gender	Zipcode	Disease
Andre	1/21/76	Female	53715	Heart Disease
Beth	4/13/86	Female	53715	Hepatitis
Carol	2/28/76	Male	53703	Brochitis
Dan	1/21/76	Male	53703	Broken Arm
Ellen	4/13/86	Female	53806	Flu
Eric	2/28/76	Female	53806	Hang Nail

a tuple

- The information for each respondent contained in the released data set cannot be distinguished from at least  $k - 1$  individuals
- Each tuple of quasi-identifier values in the released table must appear in at least  $k$  records

# $k$ -Anonymity

original table

date of birth

Name	DOB	Gender	Zipcode	Disease
Andre	1/21/76	Female	53715	Heart Disease
Beth	4/13/86	Female	53715	Hepatitis
Carol	2/28/76	Male	53703	Brochitis
Dan	1/21/76	Male	53703	Broken Arm
Ellen	4/13/86	Female	53806	Flu
Eric	2/28/76	Female	53806	Hang Nail

2-anonymous  
table

DOB	Gender	Zipcode	Disease
*	Female	5371*	Heart Disease
*	Female	5371*	Hepatitis
*	Male	5370*	Brochitis
*	Male	5370*	Broken Arm
*	Female	538**	Flu
*	Female	538**	Hang Nail

# Limitations of $k$ -anonymity

## Original microdata

QID				SA
Zipcode	Age	Sex	Disease	
47676	27	F	Ovarian Cancer	
47602	22	F	Ovarian Cancer	
47678	27	M	Ovarian Cancer	
47905	43	M	Heart disease	
47909	52	F	Cancer	
47906	47	M	Cancer	

Alice → (points to the first row)

Naroto → (points to the fourth row)

## 3-anonymous table

QID			SA
Zipcode	Age	Sex	Disease
476**	2*	*	Ovarian Cancer
476**	2*	*	Ovarian Cancer
476**	2*	*	Ovarian Cancer
4790*	[43,52]	*	Heart disease
4790*	[43,52]	*	Cancer
4790*	[43,52]	*	Cancer

- Suppose that the adversary knows Alice's combination of quasi-identifier attributes is (47676, 27, F). The attacker does not know which of the first 3 records corresponds to Alice's record, but learns her health condition is cancer
  - Homogeneity attack**
- Suppose that the adversary knows Naroto's combination of quasi-identifier attributes is (47905, 47, M). The attacker learns the last record is probably Naroto's as Japanese people have low incidence of heart attacks
  - Background knowledge attack**

# Limitations of $k$ -anonymity

- It prevents identity disclosure
  - The attacker cannot find out which record corresponds to a given respondent
  - however, from the previous examples, it is prone to homogeneity and background-knowledge attacks
    - **no privacy at all**
- But not (sensitive or confidential) attribute disclosure
  - The adversary cannot tell that a given person has a certain sensitive attribute
- Assumes which information is available for linkage or which not

# $p$ -Sensitive, $k$ -anonymity

3-sensitive, 6-anonymous table

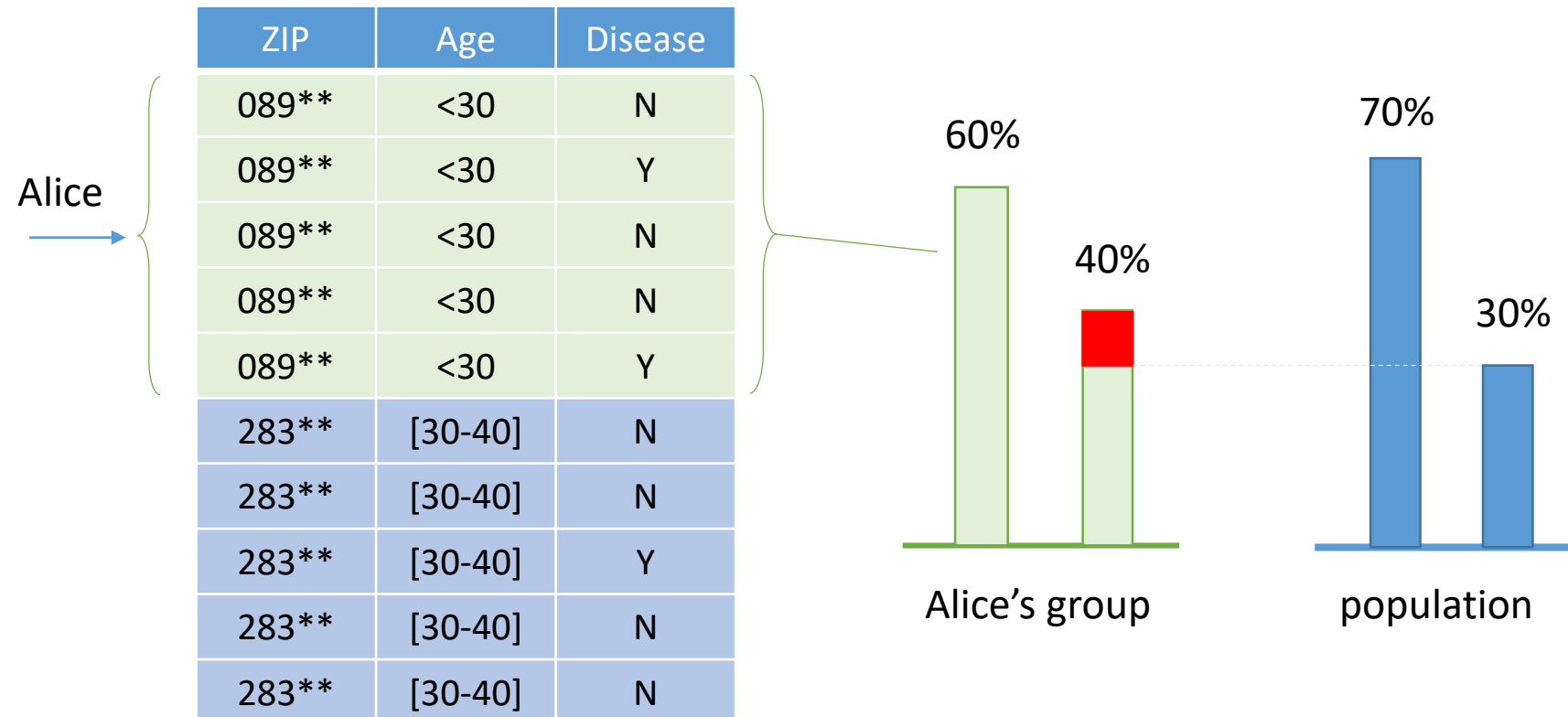
Caucas	787XX	Flu
Caucas	787XX	Shingles
Caucas	787XX	Acne
Caucas	787XX	Flu
Caucas	787XX	Acne
Caucas	787XX	Flu
Asian/AfrAm	78XXX	Flu
Asian/AfrAm	78XXX	Flu
Asian/AfrAm	78XXX	Acne
Asian/AfrAm	78XXX	Shingles
Asian/AfrAm	78XXX	Acne
Asian/AfrAm	78XXX	Flu

at least 3 different values  
of the confidential attribute

- Aimed to protect against confidential attribute disclosure
- The idea is to have at least  $p$  different sensitive values of the confidential attribute within each  $k$ -anonymous class

# Limitations of $p$ -sensitive, $k$ -anonymity

- Prone to skewness attacks



# $l$ -Diversity

- The idea is that the sensitive attributes are “diverse” within each  $k$ -anonymous group
- Each equivalence class has at least  $l$  well-represented sensitive values
- Different meanings of “well-represented” values, in addition to distinct  $l$ -diversity
  - **Entropy  $l$ -diversity.** The entropy of the distribution of sensitive values in each equivalence class is at least  $\log l$

$$H(Z|X = x) = - \sum_z p_{Z|X}(z|x) \log p_{Z|X}(z|x) \geq \log l \quad \text{for all class } x$$

entropy of the confidential attribute  $Z$   
on the equivalent class  $x$

parameter

# Limitations of $l$ -diversity

- Still vulnerable to skewness attacks
- And similarity attacks...

## 3-diverse, 3-anonymous table

QID			SA
Zipcode	Age	Sex	Disease
476**	2*	*	Lung Cancer
476**	2*	*	Prostate Cancer
476**	2*	*	Bladder Cancer
4790*	[43,52]	*	Heart disease
4790*	[43,52]	*	Flu
4790*	[43,52]	*	Diabetes



# t-Closeness

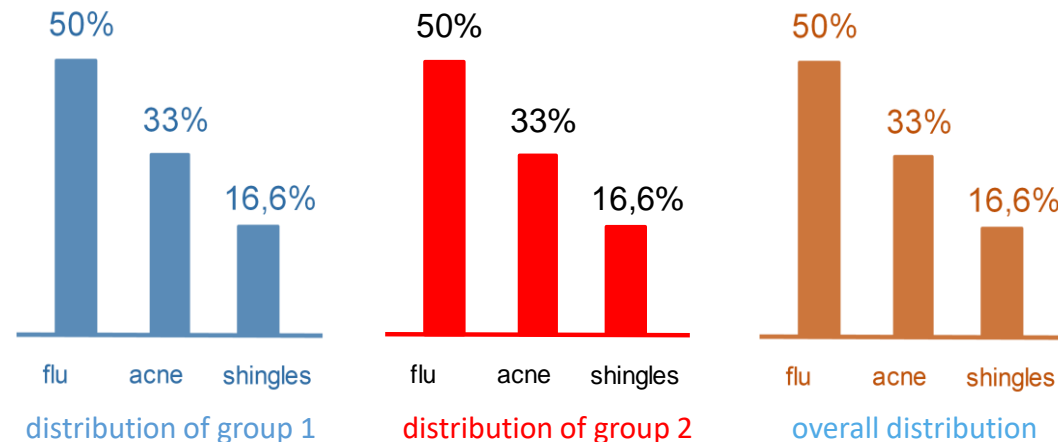
Caucas	787XX	Flu
Caucas	787XX	Shingles
Caucas	787XX	Acne
Caucas	787XX	Flu
Caucas	787XX	Acne
Caucas	787XX	Flu
Asian/AfrAm	78XXX	Flu
Asian/AfrAm	78XXX	Flu
Asian/AfrAm	78XXX	Acne
Asian/AfrAm	78XXX	Shingles
Asian/AfrAm	78XXX	Acne
Asian/AfrAm	78XXX	Flu

overall distribution

- The idea is that the **distribution** of confidential attributes given perturbed key attributes observed must be close to the **entire distribution** of the confidential attribute

$$|d(p_{Z|X}(z|x), p_Z(z))| \leq t$$

confidential      group or equivalence class



# But how!?

Mechanisms to enforce data similarity (syntactic privacy notions)

# Queryable databases protection

- Query perturbation
  - Deterministically correct answers **not needed**
  - Input vs output perturbation
- Query restriction
  - **Deterministically correct answers** and **exact** are needed
  - Refuse to answer to sensitivity queries
- Camouflage
  - **Deterministically correct answers** but **non-exact** are okay
  - Small interval answers of each confidential value

# Brief overview of methods for tabular data

## ■ Non-perturbative

- Do not perturb or modify the values in the tables, but may eliminate or suppress them. Example include **cell suppression** through sensitive rules

## ■ Perturbative

- Output a table with some modified values. Examples include **controlled rounding** and controlled tabular adjustment

	Italian	Spanish	Total
City1	2	7	9
City2	5	12	17
City3	12	0	12
Total	19	19	38

	Italian	Spanish	Total
City1	0	10	10
City2	5	10	20
City3	10	0	10
Total	15	20	40

rounding base 5

# Microdata protection

- Microdata are matrices of respondents per attributes
  - Numerical (e.g., weight, salary) or categorical (e.g., gender, job)

Identifiers	Key Attributes		Confidential Attributes
	Height	Weight	High Cholesterol
John Smith	5'4"	158	Y
Tang Lee	5'3"	162	Y
Luis Melo	5'6"	161	Y
Anna Frank	5'8"	157	N

# Microdata protection

- Identifiers are removed, obviously
- QIs can be used to **record linkage** but they possess high **analytical value**
- Therefore anonymization algorithms **must address QIs**
  - privacy-utility trade-off

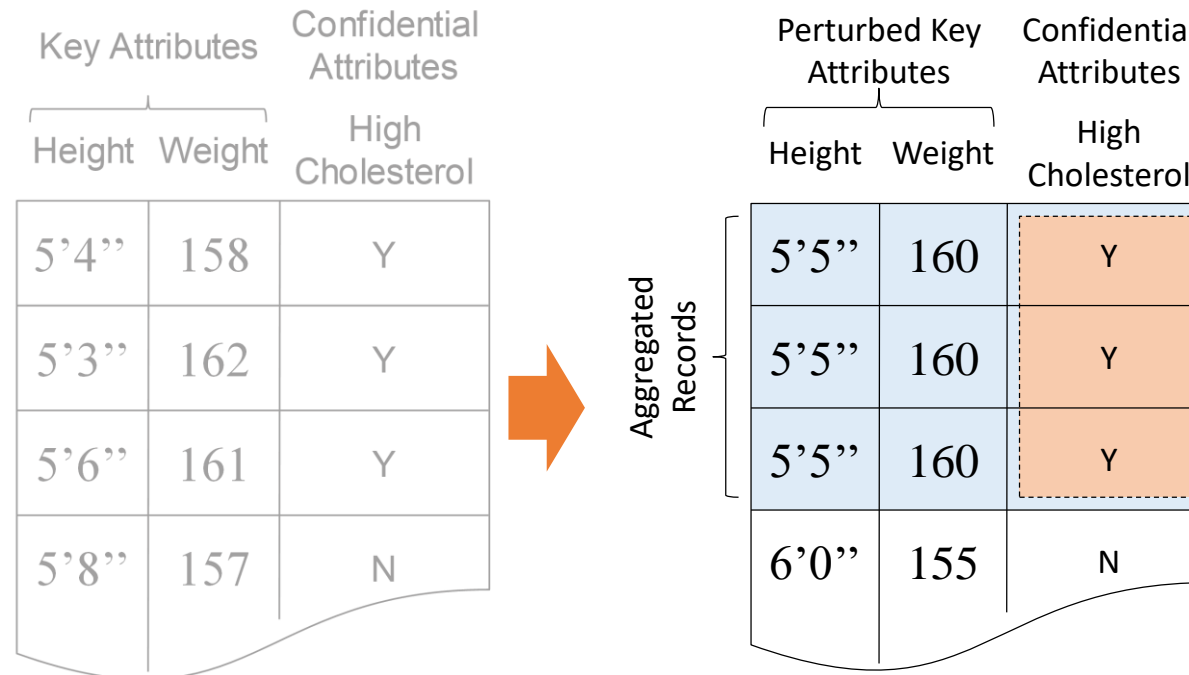
Key Attributes		Confidential Attributes
Height	Weight	High Cholesterol
5'4"	158	Y
5'3"	162	Y
5'6"	161	Y
5'8"	157	N

# Methods for microdata protection

- **Masking** methods: generate a modified version of the original data
  - **Perturbative**: modify data
    - Noise addition, microaggregation, rank swapping, microdata rounding, and resampling
  - **Non-perturbative**: do not modify the data but rather produce partial suppressions or reductions of detail in the original dataset
    - Sampling, global recoding, top and bottom coding, and local suppression
- **Synthetic** methods: generate synthetic or artificial data with **similar statistical properties**

# Perturbation: Microaggregation

- Mask by grouping and replacement by “mean” value




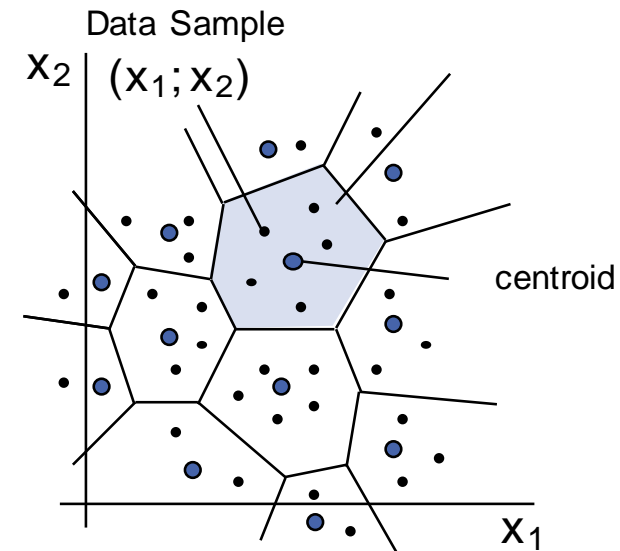


# Perturbation: Microaggregation (ctd.)

- The optimal  $k$ -partition is the one maximizing the **within-group homogeneity**
  - The higher the within-group homogeneity, the lower the information loss
- A typical criterion to measure homogeneity in clustering is the **sum of squared errors (SSE)**

$$SSE = \sum_{i=1}^g \sum_{j=1}^{n_i} (x_{ij} - \bar{x}_i)' (x_{ij} - \bar{x}_i)$$


  
 centroid



# Perturbation: Data swapping

- The idea is to transform a database by **exchanging** values of **confidential attributes** among individual records
- Information loss is not reduced but may refrain participants to contribute their data

Variable	Original data			After perturbing the data		
ID	Gender	Region	Education	Gender	Region	Education
1	female	rural	higher	female	rural	higher
2	female	rural	higher	female	rural	lower
3	male	rural	lower	male	rural	lower
4	male	rural	lower	female	rural	lower
5	female	urban	lower	male	urban	higher
6	female	urban	lower	female	urban	lower



# Perturbative masking – Noise addition

- **Uncorrelated** noise addition
  - Neither variances nor correlations are preserved
- **Correlated** noise addition
  - Means and correlations can be preserved
- Noise addition and **linear** transformation
- Noise addition and **non-linear** transformation

# Perturbation: Differential privacy for microdata

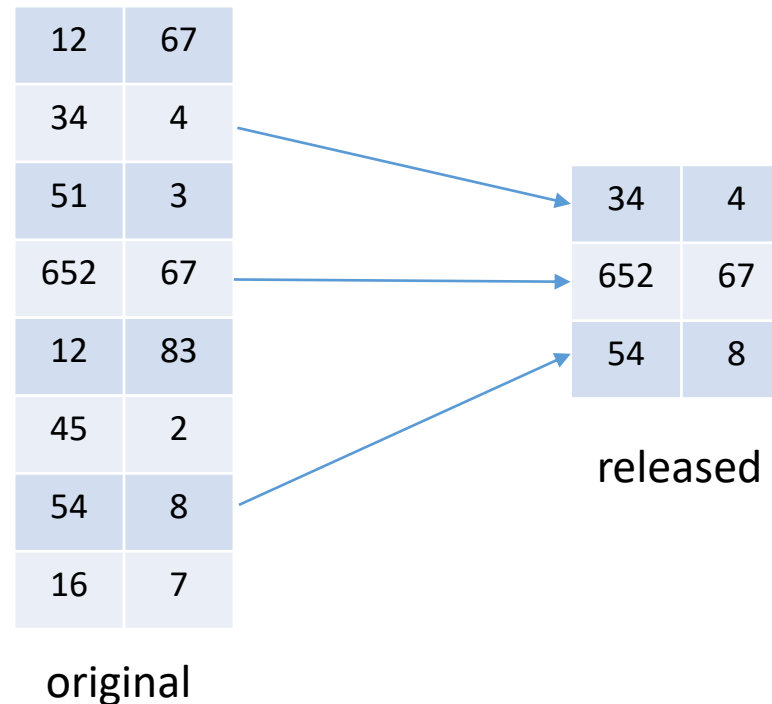
- Non-interactive scenario. Microdata available for any use without restrictions (publish tables of microdata with DP guarantees)

We'll go there later, just briefly:

- DP mechanisms are tied to **query functions**, depend on their **sensitivity**
- **Naïve** approach to generate DP microdata with the identity function
  - Collection of responses to the query “**What's the content of the  $i$ -th record of the microdata for  $i = 1, \dots, n$  ?**”
  - L1-sensitivity of the identity function?

# Non-Perturbative Masking: Sampling

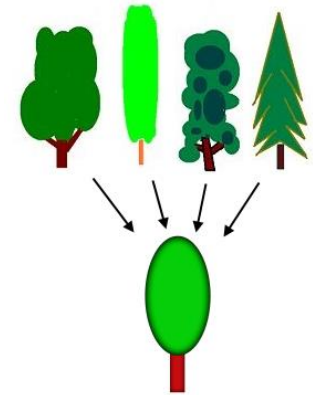
- Publish random sample of the original set of records
- Correlation determines which properties are retained (uncorrelated: none)
- Continuous numerical data need further protection



# Non-Perturbative: Generalization/Coarsening

- Reduce detail of information
- Remove least-significant parts, preserve significant, but general information

	172.169.2.132			172.169.0.0
	172.169.3.157			172.169.0.0
	145.42.124.31			145.42.0.0
	172.169.3.131			172.169.0.0
	145.42.19.31			145.42.0.0



# Non-perturbative Masking: Global recoding

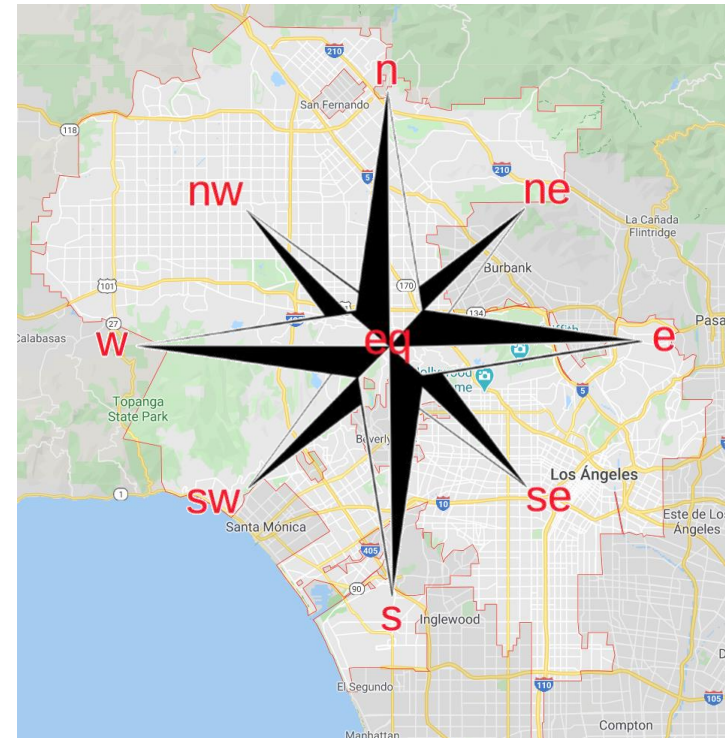
- Combine several categories of a categorical attribute or construct intervals for continuous variables
- Reduction of the level of detail and potentially the disclosure risk

A–L [ edit ]

<ul style="list-style-type: none"><li>• Angelino Heights<sup>[10]</sup></li><li>• Angeles Mesa</li><li>• Angelus Vista</li><li>• Arleta<sup>[MLA][TQ]</sup></li><li>• Arlington Heights<sup>[MLA]</sup></li><li>• Arts District<sup>[1]</sup></li><li>• Atwater Village<sup>[MLA]</sup></li><li>• Baldwin Hills<sup>[10]</sup></li><li>• Baldwin Hills/Crenshaw<sup>[MLA]</sup></li><li>• Baldwin Village<sup>[10]</sup></li><li>• Baldwin Vista<sup>[2]</sup></li><li>• Beachwood Canyon<sup>[3]</sup></li><li>• Bel Air, Bel-Air or Bel Air Estates<sup>[MLA][TQ]</sup></li><li>• Benedict Canyon<sup>[4]</sup></li><li>• Beverly Crest<sup>[MLA]</sup></li><li>• Beverly Glen<sup>[10]</sup></li><li>• Beverly Grove<sup>[MLA]</sup></li></ul>	<ul style="list-style-type: none"><li>• Beverly Hills Post Office<sup>[5]</sup></li><li>• Beverly Park<sup>[5]</sup></li><li>• Beverlywood<sup>[MLA]</sup></li><li>• Boyle Heights<sup>[MLA][TQ]</sup></li><li>• Brentwood<sup>[MLA][TQ]</sup></li><li>• Brentwood Circle<sup>[7]</sup></li><li>• Brentwood Glen<sup>[9]</sup></li><li>• Broadway-Manchester<sup>[MLA]</sup></li><li>• Brookside</li><li>• Bunker Hill<sup>[1]</sup></li><li>• Cahuenga Pass<sup>[10]</sup></li><li>• Canoga Park<sup>[MLA][TQ]</sup></li><li>• Canterbury Knolls<sup>[9]</sup></li><li>• Carthay<sup>[MLA]</sup></li><li>• Castle Heights</li><li>• Central-Alameda<sup>[MLA]</sup></li><li>• Central City<sup>[10]</sup></li></ul>	<ul style="list-style-type: none"><li>• Century City<sup>[ML]</sup></li><li>• Chatsworth<sup>[ML]</sup></li><li>• Chesterfield St</li><li>• Cheviot Hills<sup>[ML]</sup></li><li>• Chinatown<sup>[MLA]</sup></li><li>• Civic Center<sup>[1C]</sup></li><li>• Crenshaw<sup>[10]</sup></li><li>• Crestwood Hill</li><li>• Cypress Park<sup>[8]</sup></li><li>• Del Rey<sup>[MLA][TQ]</sup></li><li>• Downtown<sup>[MLA]</sup></li><li>• Eagle Rock<sup>[10]</sup></li><li>• East Gate Bel</li><li>• East Hollywood</li><li>• East Los Ange</li><li>• Echo Park<sup>[MLA]</sup></li><li>• Edendale<sup>[12]</sup></li></ul>
---	--	--

M–Z [ edit ]

<ul style="list-style-type: none"><li>• Manchester Square<sup>[MLA]</sup></li><li>• Mandeville Canyon<sup>[26]</sup></li><li>• Marina Peninsula<sup>[27]</sup></li><li>• Mar Vista<sup>[MLA][TQ]</sup></li><li>• Melrose Hill<sup>[28]</sup></li><li>• Mid-City<sup>[MLA][TQ]</sup></li><li>• Mid-Wilshire<sup>[MLA]</sup></li><li>• Miracle Mile<sup>[10]</sup></li><li>• Mission Hills<sup>[MLA][TQ]</sup></li><li>• Montecito Heights<sup>[MLA][TQ]</sup></li><li>• Monterey Hills<sup>[29]</sup></li><li>• Mount Olympus<sup>[10]</sup></li><li>• Mount Washington<sup>[MLA][TQ]</sup></li><li>• Nichols Canyon<sup>[30]</sup></li><li>• NoHo Arts District<sup>[31]</sup></li><li>• North Hills<sup>[MLA][TQ]</sup></li><li>• North Hollywood<sup>[MLA][TQ]</sup></li></ul>	<ul style="list-style-type: none"><li>• Northridge<sup>[MLA][TQ]</sup></li><li>• North University Park<sup>[10]</sup></li><li>• Old Bank District<sup>[1]</sup></li><li>• Outpost Estates<sup>[32]</sup></li><li>• Pacific Palisades<sup>[MLA][TQ]</sup></li><li>• Pacoima<sup>[MLA][TQ]</sup></li><li>• Palms<sup>[MLA][TQ]</sup></li><li>• Panorama City<sup>[MLA][TQ]</sup></li><li>• Park La Brea<sup>[10]</sup></li><li>• Picfair Village<sup>[33]</sup></li><li>• Pico Robertson<sup>[34]</sup></li><li>• Pico-Union<sup>[MLA]</sup></li><li>• Platinum Triangle<sup>[citation needed]</sup></li><li>• Playa del Rey<sup>[10]</sup></li><li>• Playa Vista<sup>[MLA]</sup></li><li>• Porter Ranch<sup>[MLA][TQ]</sup></li><li>• Rancho Park<sup>[MLA][TQ]</sup></li></ul>	<ul style="list-style-type: none"><li>• Reseda<sup>[MLA][TQ]</sup></li><li>• Reynier Village</li><li>• Rose Hills</li><li>• Rustic Canyon</li><li>• San Pedro<sup>[MLA]</sup></li><li>• Sawtelle<sup>[MLA][TQ]</sup></li><li>• Shadow Hills<sup>[M]</sup></li><li>• Sherman Oaks</li><li>• Sherman Villa</li><li>• Silver Lake<sup>[MLA]</sup></li><li>• Skid Row<sup>[37]</sup></li><li>• Solano Canyon</li><li>• South Central</li><li>• South Park<sup>[MLA]</sup></li><li>• South Roberts</li><li>• Spaulding Squ</li><li>• Studio City<sup>[MLA]</sup></li></ul>
--	--	---



Source: Wikipedia, Google Maps

# Non-perturbative Masking: Local suppression

- Eliminate certain values of individual attributes so as to increase the number of records sharing a combination of key-attribute values
- Oriented to categorical attributes

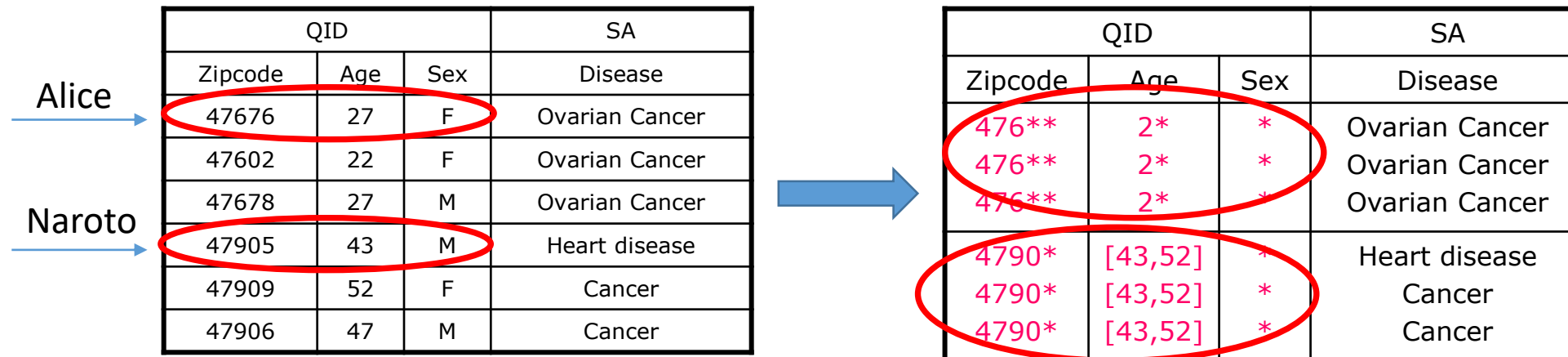
North	[20-30]
South	[30-40]
South	[20-30]
South-West	[20-30]
East	[30-40]
South-West	[30-40]
South	[50-60]
East	[20-30]

***	[20-30]
South	[30-40]
South	[20-30]
South-West	[20-30]
East	[30-40]
South-West	[30-40]
South	[50-60]
East	[20-30]



# Intermediate Summary of Masking

- Attempt to adapt microdata to achieve privacy notion
  - (Recall k-anonymity, ...)
- Potentially quite complex optimization problem with many degrees of freedom



# Synthetic microdata generation

- **Masking** methods: generate a modified version of the original data
  - Perturbative: modify data
    - Noise addition, microaggregation, rank swapping, microdata rounding, and resampling
  - Non-perturbative: do not modify the data but rather produce partial suppressions or reductions of detail in the original dataset
    - Sampling, global recoding, top and bottom coding, and local suppression
- **Synthetic** methods: generate synthetic or artificial data with **similar statistical properties**

# Synthetic microdata generation

- Extract chosen, preserved statistics from microdata (probabilities, distributions, ML models)
- Randomly generate data (sampling, transformation)
- Pros:
  - Possibility to generate “unlimited” data sets
  - seem to address the reidentification problem, as data are “synthetic”
- Cons:
  - Published synthetic records can match an individual’s data, if model is not private
  - Data utility limited to the statistics captured by the model

# Summary

- Tabular, queryable and microdata formats
- SDC aims to protect individuals privacy while providing useful statistical information
- A common classification for mechanisms is perturbative and non-perturbative
  - Perturbative mechanisms modify the data, while non-perturbative mechanisms produce partial suppressions or reductions of detail of the data
  - Generation of synthetic data (not usually private)